

Integrated Simulations of Energetic Particle-driven Modes in Burning Plasmas

Guo-Yong Fu
Princeton Plasma Physics Laboratory

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Outline

- Hybrid model of M3D
- Highlights of M3D Hybrid Simulations
- Issues for integrated simulation of energetic particle-driven modes in burning plasmas

M3D XMHD Model

$$\rho \frac{d\mathbf{v}}{dt} + \rho(\mathbf{v}_i^* \cdot \nabla)\mathbf{v}_\perp = -\nabla P - \nabla \cdot \mathbf{P}_h + \mathbf{J} \times \mathbf{B} - \nabla \cdot \Pi_i$$

$$\rho \frac{d\mathbf{v}}{dt} = -\nabla P - \nabla \cdot \mathbf{P}_h + \mathbf{J} \times \mathbf{B}$$

$$\mathbf{J} = \nabla \times \mathbf{B}, \quad \frac{\partial \mathbf{B}}{\partial t} = -\nabla \times \mathbf{E}$$

$$\mathbf{E} + \mathbf{v} \times \mathbf{B} = \eta \mathbf{J} - \nabla_{\parallel} P_e / en - \mathbf{b}\mathbf{b} \cdot \nabla \cdot \Pi_e$$

$$\partial P / \partial t + \mathbf{v} \cdot \nabla P = -\gamma P \nabla \cdot \mathbf{v} + \dots$$

$$\partial P_e / \partial t + \mathbf{v} \cdot \nabla P_e = -\gamma P_e \nabla \cdot \mathbf{v} + \dots$$

CGL pressure and gyrokinetic equations

- Pressure tensor

$$\mathbf{P}_h = P_\perp \mathbf{I} + (P_\parallel - P_\perp) \mathbf{b}\mathbf{b}$$

$$f = \sum_i \delta(\mathbf{R} - \mathbf{R}_i) \delta(v_\parallel - v_{\parallel,i}) \delta(\mu - \mu_i)$$

- Gyrokinetic Equations

$$\frac{d\mathbf{R}}{dt} = \frac{1}{B^{**}} \left[v_\parallel (\mathbf{B}^* - \mathbf{b}_0 \times (\langle \mathbf{E} \rangle - \frac{1}{q} \mu \nabla (B_0 + \langle \delta B \rangle))) \right]$$

$$m \frac{dv_\parallel}{dt} = \frac{q}{B^{**}} \mathbf{B}^* \cdot (\langle \mathbf{E} \rangle - \frac{1}{q} \mu \nabla (B_0 + \langle \delta B \rangle))$$

$$\mathbf{B}^* = \mathbf{B}_0 + \langle \delta \mathbf{B} \rangle + \frac{mv_\parallel}{q} \nabla \times \mathbf{b}_0, \quad B^{**} = \mathbf{B}^* \cdot \mathbf{b}_0$$

Highlights of Recent M3D Hybrid Simulations

- $n=1$ mode in ITER;
- Fishbone nonlinear evolution in tokamak;
- Beam-driven Alfvén modes in NSTX;

Ref: G.Y. Fu et al., IAEA Fusion Energy Conference, 2004.

H.R. Strauss et al, Nucl. Fusion 44, 1008 (2004).

G.Y. Fu et al., Phys. Plasma 13, 052517, 2006.

n=1 mode in ITER

Importance of shaping effects on alpha particle stabilization of internal kink;

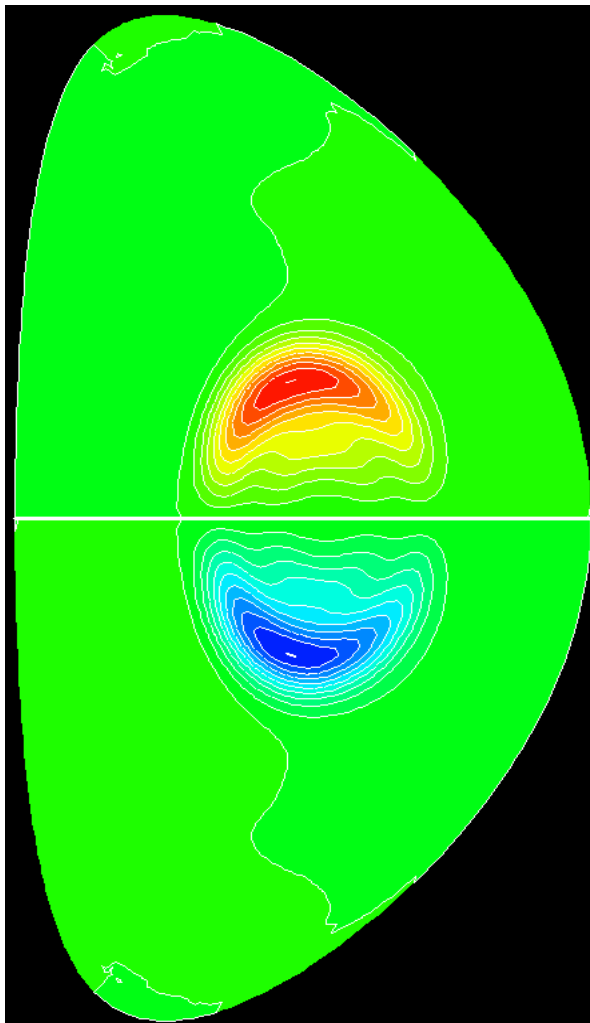
fishbone stability is marginal;

Ion kinetic effects are strongly stabilizing.

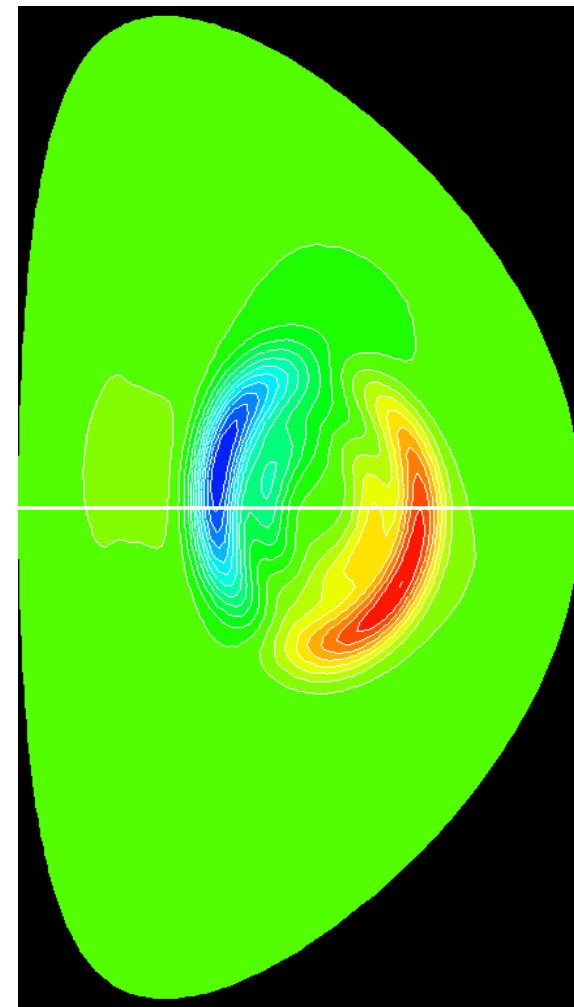
Alpha Particle Stabilization of Internal Kink Mode for ITER:

Internal Kink Mode Structure

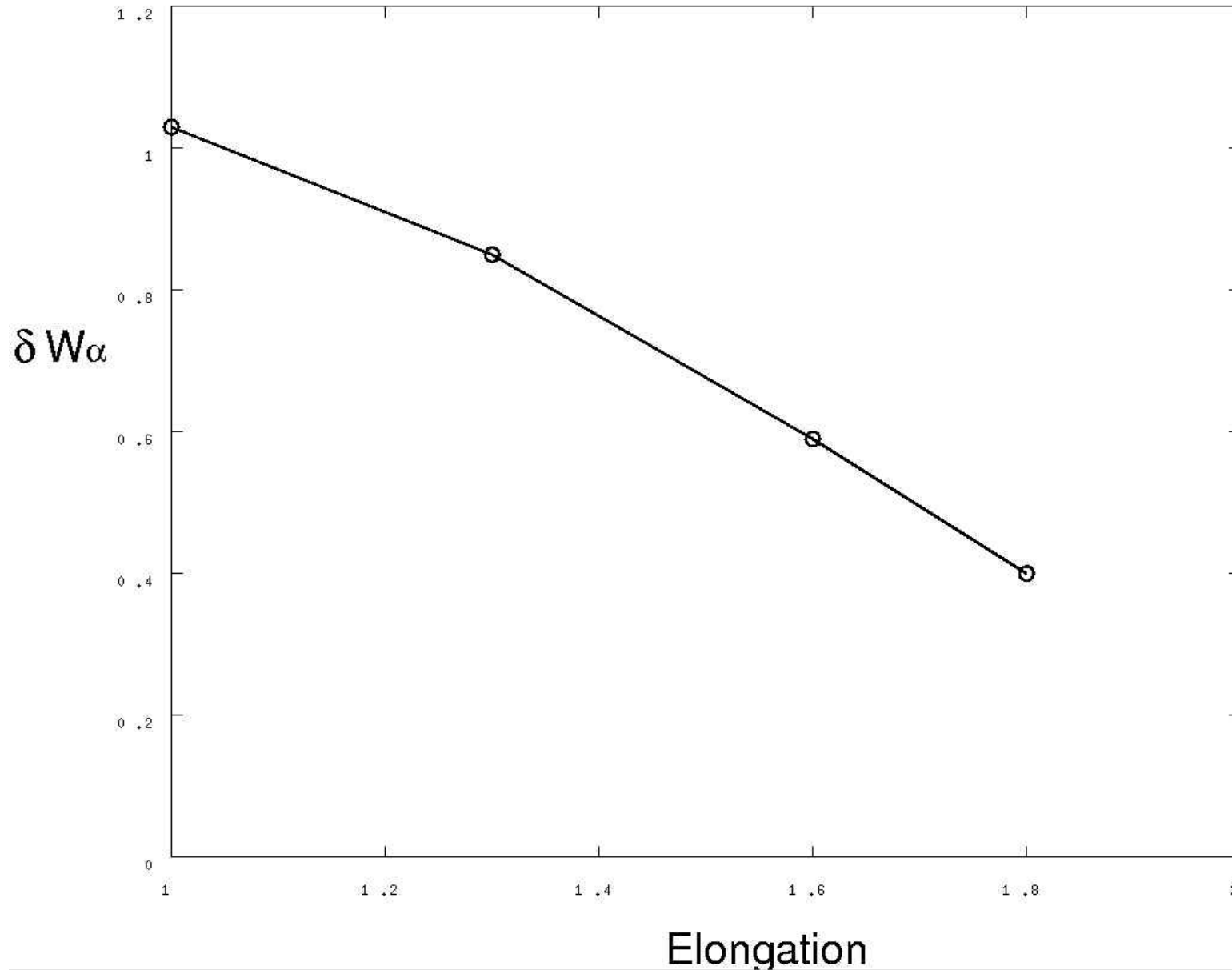
$\beta_\alpha=0.0$



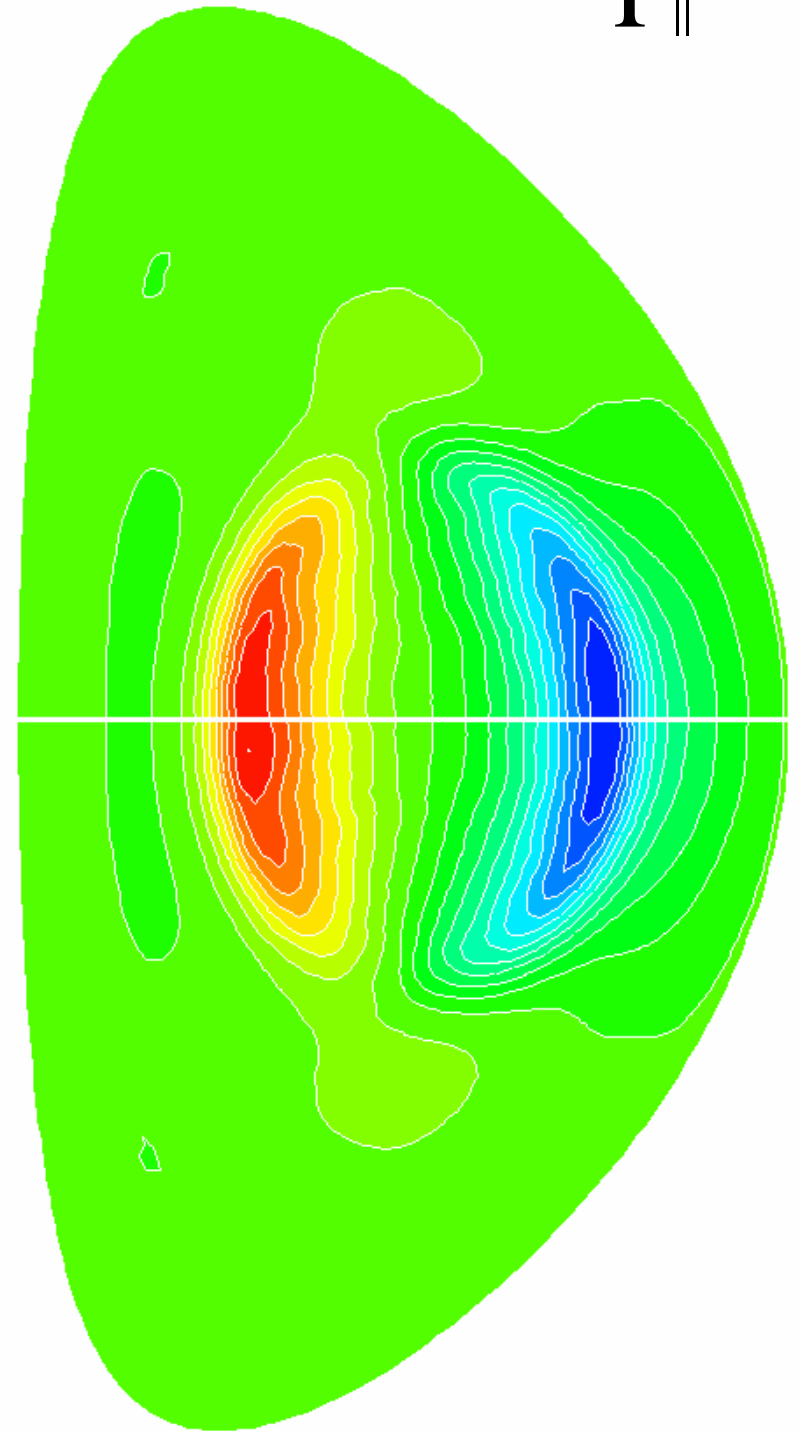
$\beta_\alpha=1.0\%$



Plasma shaping reduces alpha particle stabilization significantly



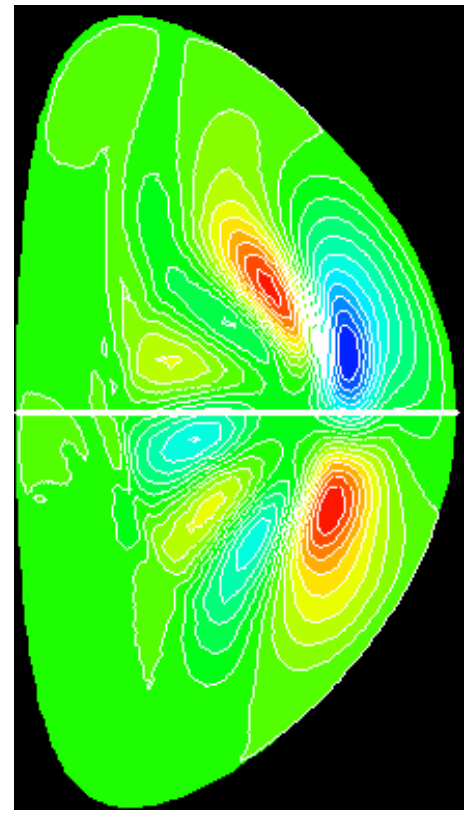
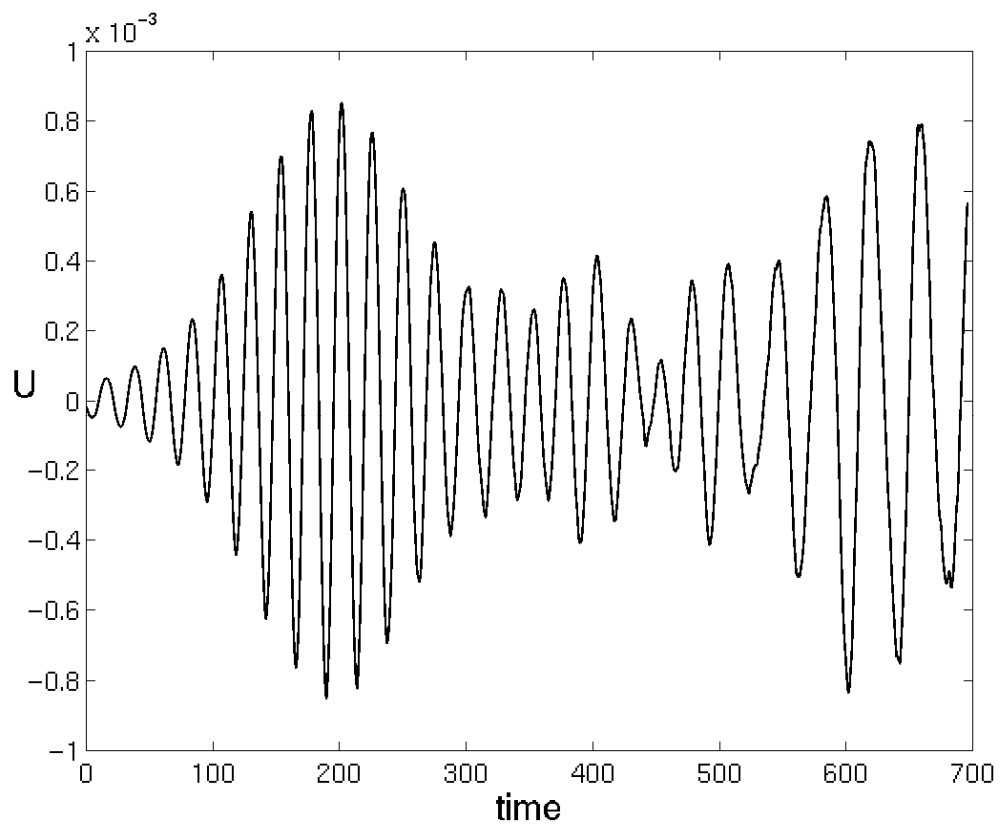
Thermal ion kinetic effects
reduce MHD growth rate
by half (Kruskal-Oberman)



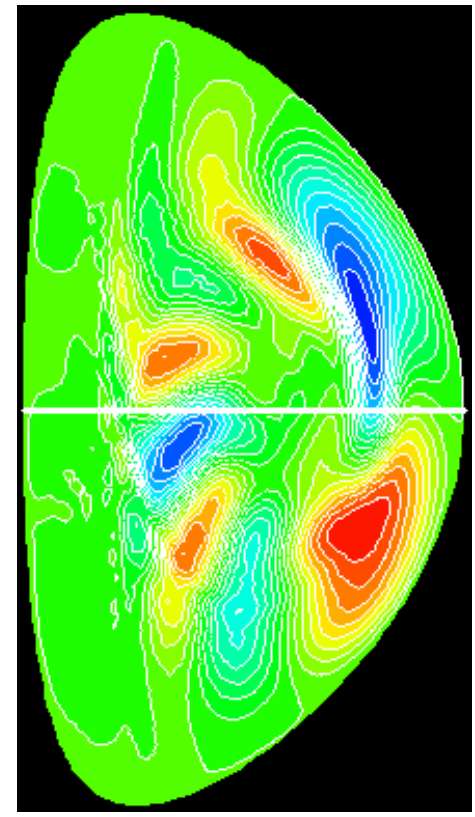
Beam-driven Alfvén modes in NSTX

- TAE frequency chirping
- Multi-mode simulations show significant effects from mode-mode coupling;

Beam-driven modes in NSTX: frequency chirping

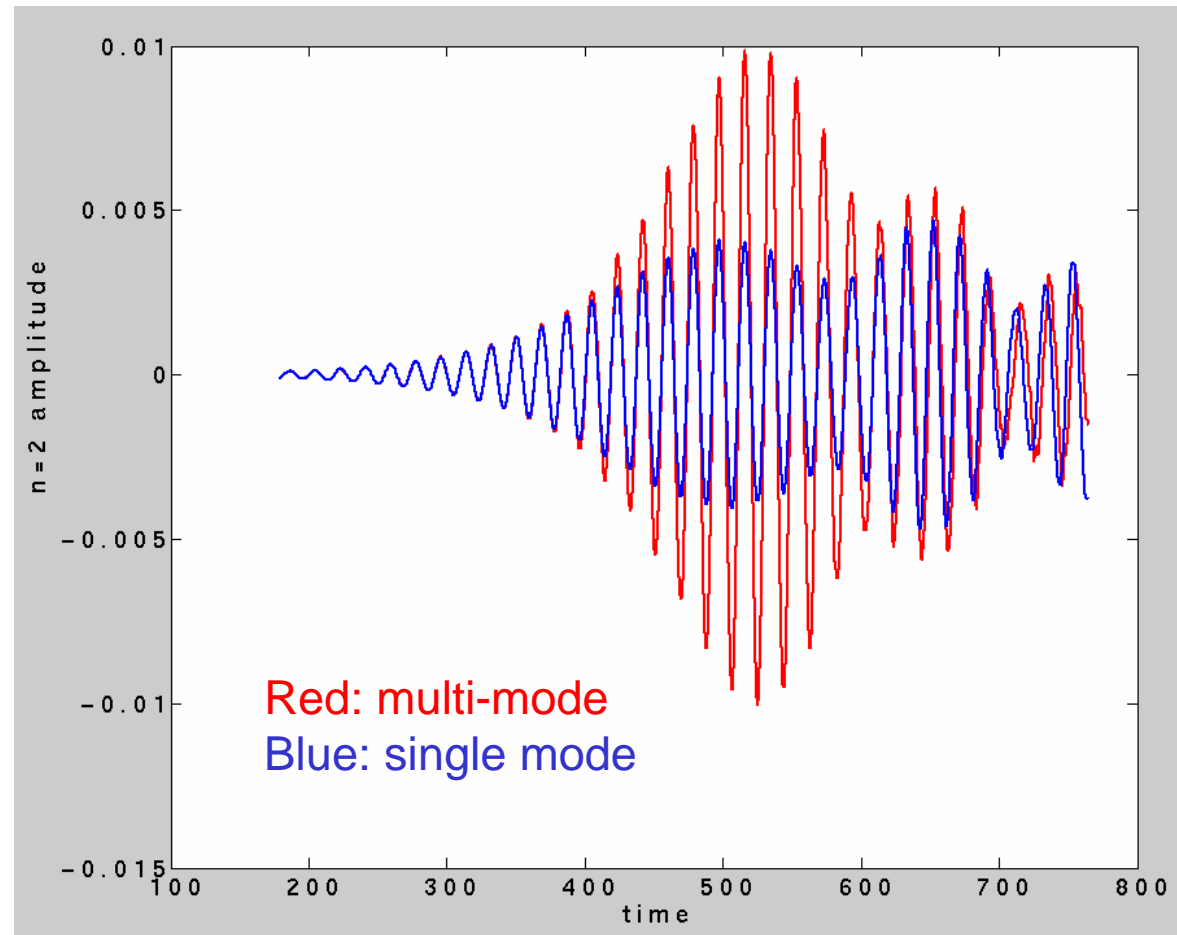
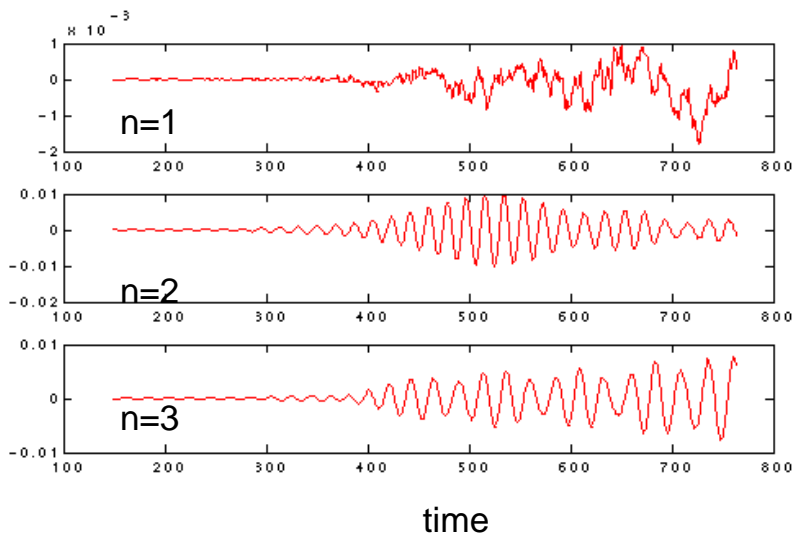
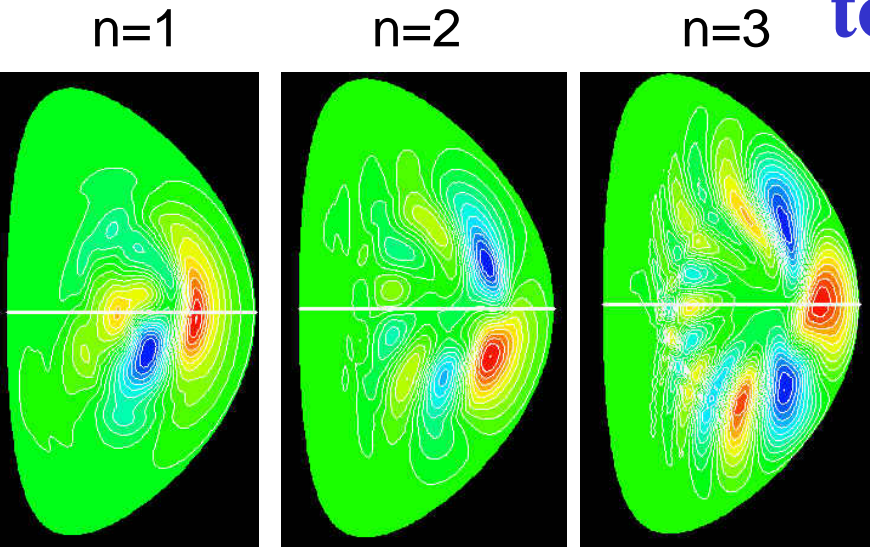


$t=0.0$

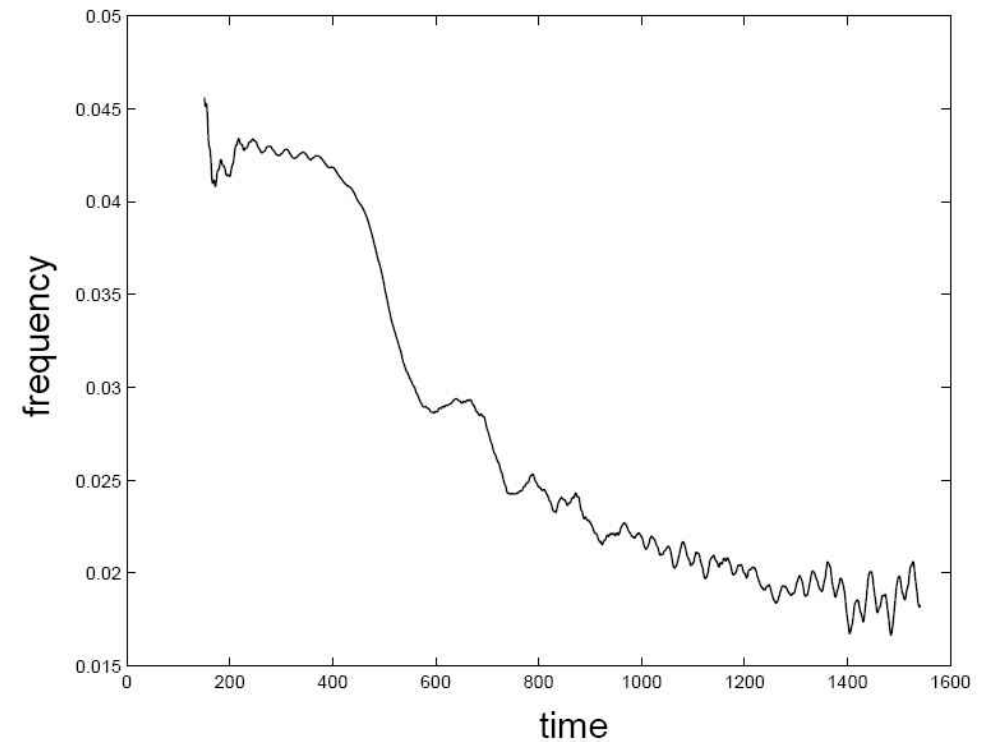
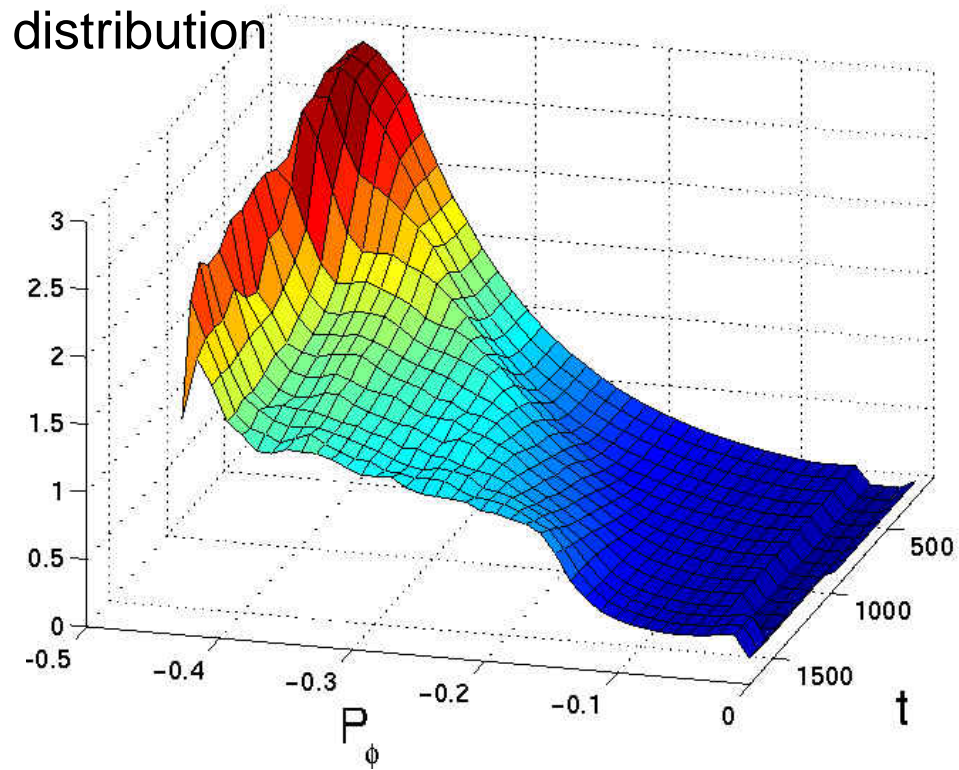


$t=336$

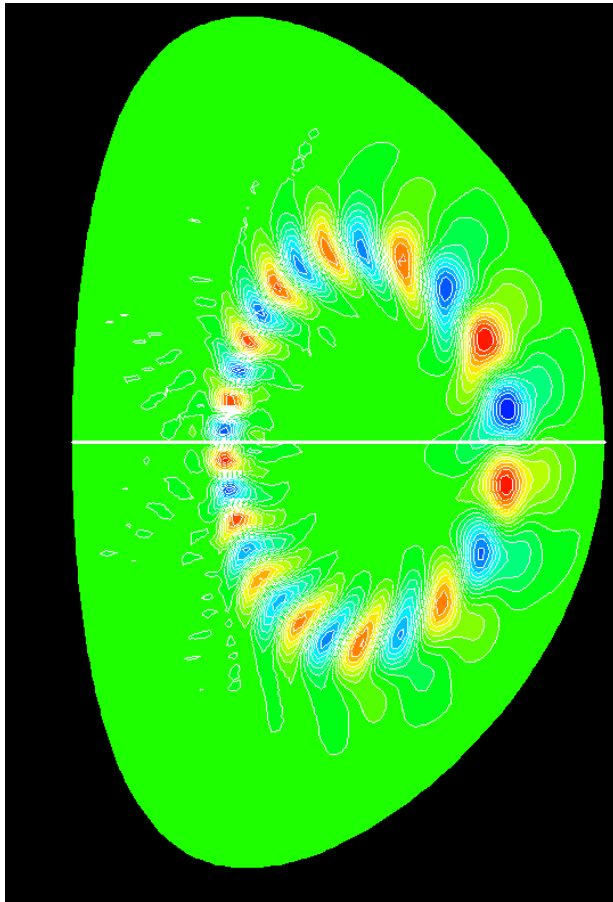
Multi-mode simulations of beam-driven Alfvén modes show strong interaction between different toroidal modes



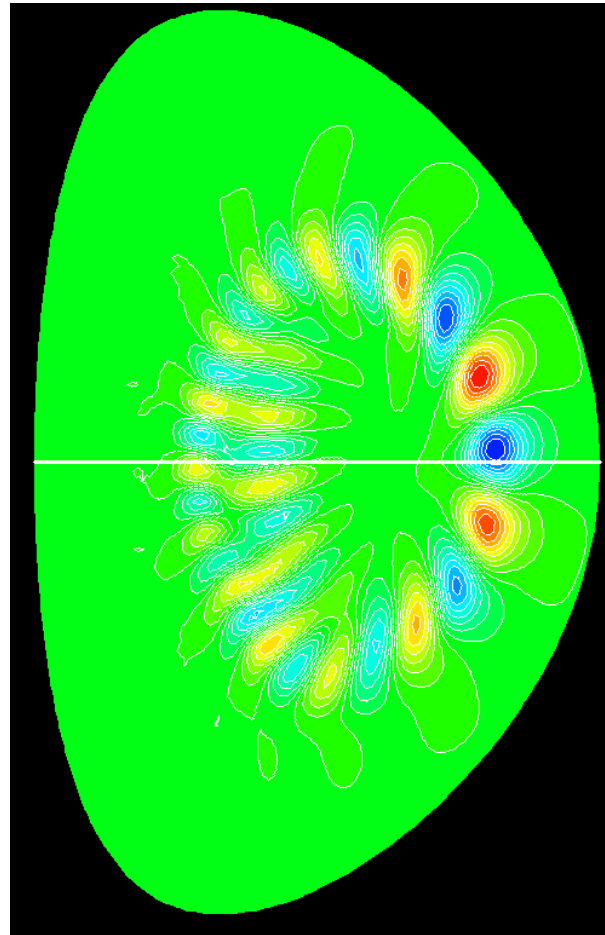
Simulation of fishbone shows distribution fattening and strong frequency chirping



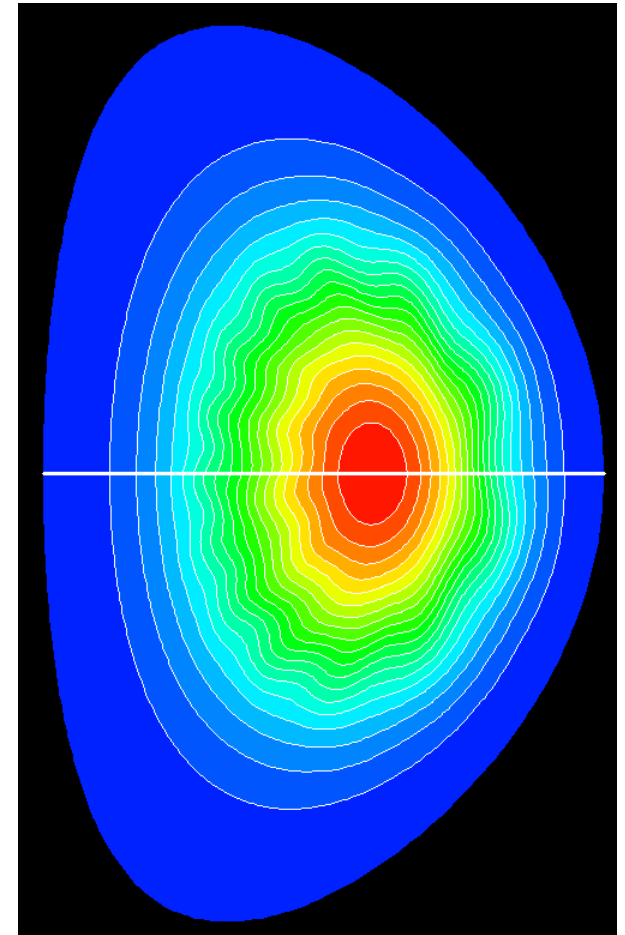
Initial simulations of Alfvén eigenmodes in reversed shear DIII-D plasmas



Velocity stream function



Pressure perturbation

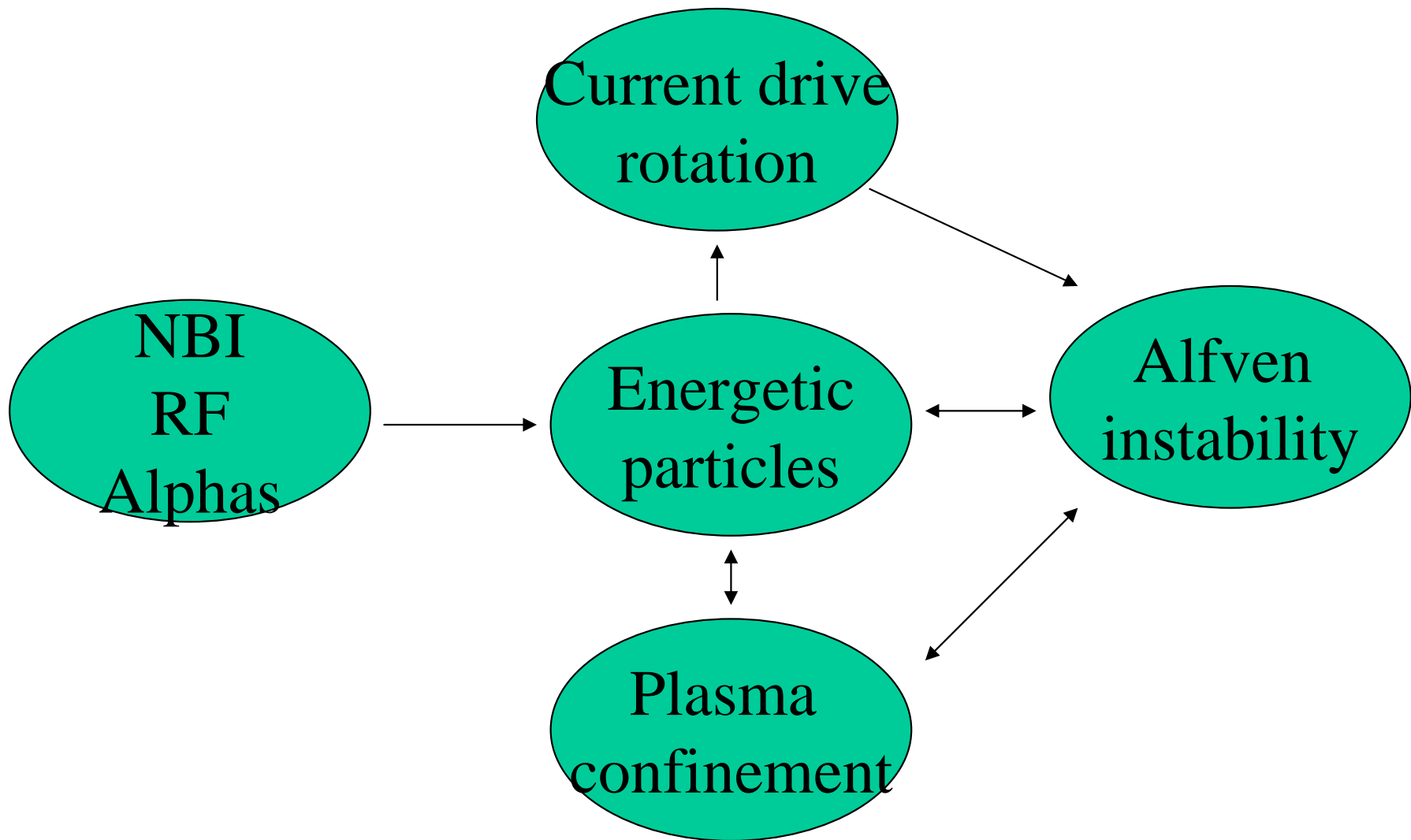


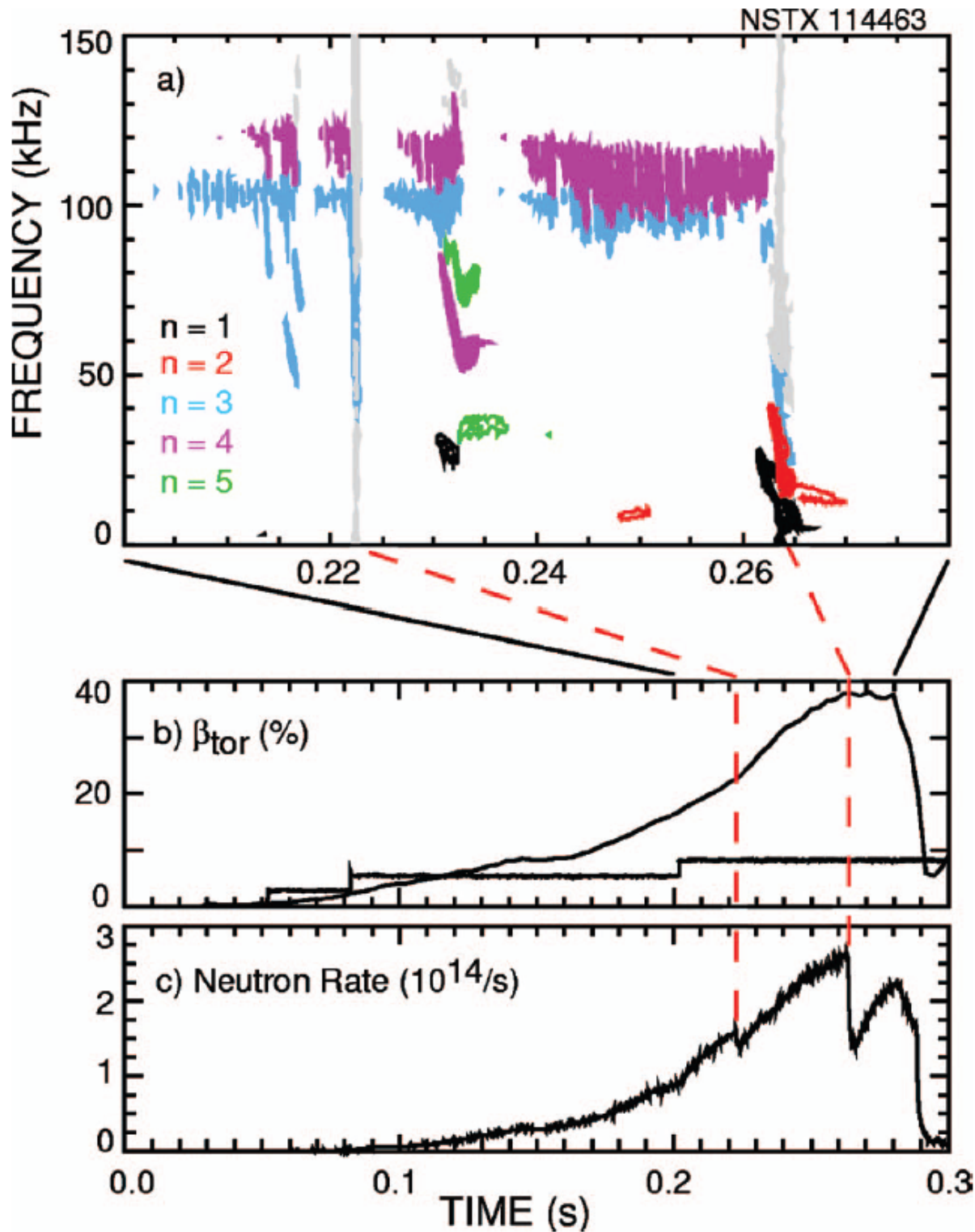
Total pressure

Future Direction for Energetic Particle Physics

- Linear Stability: basic mechanisms well understood, but lack of a comprehensive code which treats dampings and energetic particle drive non-perturbatively
- Nonlinear Physics: single mode saturation well understood, but lack of study for multi-mode dynamics
- Effects of energetic particles on thermal plasmas: needs a lot of work (integrated simulations).

Integration of Energetic Particle Physics





Experimental
motivation for
integrated
simulations

Issues for integrated simulations

- Integration of physics: kinetic MHD
- Integration of different modes
- Integration of different time scale

Integration of physics: kinetic MHD

- Alpha particle stabilization of internal kink mode;
- Energetic particle destabilization;
- FLR effects;
- Ion and electron Landau damping;

Integration of different modes

- TAE
- Fishbone/EPM
- Tearing modes
- KBM

Integration of different time scales

- Shear Alfvén time;
- Linear growth time of Alfvén eigenmodes;
- Energetic particle slowing down time and velocity diffusion time;
- Plasma confinement time;
- Equilibrium evolution time (q profile).